A possible implementation is suggested of J H Ellis’s proposed method of encryption involving no sharing of secret information (key lists, machine set-ups, pluggings etc) between sender and receiver.

**Summary**

A method for non-secret encryption (see [1] and [2]) is herein expounded. Non-secret encryption is a way of passing a message securely without the need for information (eg a machine set-up) known to the sender and recipient but not to any interceptor.

**Introduction**

The method set out below is a modification of my original idea suggested by J H Ellis. It is rather neater but presents the same problem to an interceptor as the original.

**The method**

The initial requirements for encryption are:

1. A shift register generating a linear recursive sequence of length $p$ (prime).
2. Different random number generators held by the sender and recipient.

The sender wishes to send a fill $A$ of the shift register and the encryption proceeds as follows:

a. The sender generates a random number $k$ and calculates $A^k$ which he transmits.

b. The recipient generates a random number $l$ and calculates $(A^k)^l = A^{kl}$ which he transmits.

c. The sender solves the Euclidean algorithm to find $K$ such that $Kk = 1 \pmod{p}$ and calculates $(A^{kl})^K = A^l$ which he transmits.

d. The recipient solves the Euclidean algorithm to find $L$ such that $Ll = 1 \pmod{p}$ and calculates $(A^l)^L = A$ which is the message the sender wanted to give him.

**The interceptor's problem**

The interceptor trying to read the traffic is now presented with the problem:

1. Given $A^k$, $A^l$ and $A^{kl}$, find $A$.

If he can solve the distance problem for the recursive sequence used he can find $x$, $y$, $z$ such that

- $A^k = B^x$
- $A^l = B^y$
- $A^{kl} = B^z$
(B is the basic root of the recursion) and now \( A = Bw \) where \( w = xy/z \).

Unfortunately a solution to the interceptor’s problem does not seem to yield a solution to the distance problem.

**Remarks**

1. The security of the system depends upon no one discovering a good algorithm to solve the interceptor’s problem, but any method of encryption must depend upon something of this sort.
2. \( p \) need not necessarily be prime, but if it is not, then care must be taken that \( k \) and \( l \) are coprime to \( p \).
3. The information rate of the system is low in that 3 bits are broadcast for every 1 of the message. (The ratio in the method of [2] is 2 for 1).

**References**
